# Item Specifications



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# Grade 8 Mathematics Introduction

In 2014 Missouri legislators passed House Bill 1490, mandating the development of the Missouri Learning Expectations. In April of 2016, these Missouri Learning Expectations were adopted by the State Board of Education. Groups of Missouri educators from across the state collaborated to create the documents necessary to support the implementation of these expectations.

One of the documents developed is the item specification document, which includes all Missouri grade level/course expectations arranged by domains/strands. It defines what could be measured on a variety of assessments. The document serves as the foundation of the assessment development process.

Although teachers may use this document to provide clarity to the expectations, these specifications are intended for summative, benchmark, and large-scale assessment purposes.

Components of the item specifications include:

**Expectation Unwrapped** breaks down a list of clearly delineated content and skills the students are expected to know and be able to do upon mastery of the Expectation.

**Depth of Knowledge (DOK) Ceiling** indicates the highest level of cognitive complexity that would typically be assessed on a large scale assessment. The DOK ceiling is not intended to limit the complexity one might reach in classroom instruction.

**Item Format** indicates the types of items used in large scale assessment. For each expectation, the item format specifies the type best suited for that particular expectation.

**Text Types** suggests a broad list of text types for both literary and informational expectations. This list is not intended to be all inclusive: other text types may be used in the classroom setting. The expectations were written in grade level bands; for this reason, the progression of the expectations relies upon increasing levels of quantitative and qualitative text

complexities.

**Content Limits/Assessment Boundaries** are parameters that item writers should consider when developing a large scale assessment. For example, some expectations should not be assessed on a large scale assessment but are better suited for local assessment.

**Sample stems** are examples that address the specific elements of each expectation and address varying DOK levels. The sample stems provided in this document are in no way intended to limit the depth and breadth of possible item stems. The expectation should be assessed in a variety of ways.

	Mathematics	8.NS.A.1.a
NS	Number Sense and Operations	
Α	Know that there are numbers that are not rational, and approximate them by rational numbers.	
1	Explore the real number system.	
а	Know the differences between rational and irrational numbers.	
	Expectation Unwrapped	DOK Ceiling
The stud	ant will know that all rational numbers can be written as a fraction	3
The stud	ent will know that all rational numbers can be written as a fraction.	Item Format
The stud	ent will know that all irrational numbers can be written as non-terminating, non-repeating decimals.	Selected Response
		Constructed Response
		Technology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Limit sau	are roots to less than or equal to six hundred twenty-five.	<b>NO</b> – a calculator will not be
Exclude	all fractions with a radical in the numerator or denominator	available for items

	Mathematics	8.NS.A.1.b
NS	Number Sense and Operations	
Α	Know that there are numbers that are not rational, and approximate them by rational numbers.	
1	Explore the real number system.	
b	Understand that all rational numbers have a decimal expansion that terminates or repeats.	
	Expectation Unwrapped	DOK Ceiling
The stud	dent will understand that all rational numbers have a decimal expansion that either terminates or repeats.	Selected Response Constructed Response Technology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation NO – a calculator will not be available for items

	Mathematics	8.NS.A.1.c
NS	Number Sense and Operations	·
Α	Know that there are numbers that are not rational, and approximate them by rational numbers.	
1	Explore the real number system.	
С	Convert decimals which repeat into fractions and fractions into repeating decimals.	
	Expectation Unwrapped	DOK Ceiling
The stud	ant will convert repeating decimals into fractions	3
The stud	ent will convert repeating decimals into fractions.	Item Format
The stud	ent will convert fractions into repeating decimals.	Selected Response
		Constructed Response
		rechnology Enhanced
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Sample Stems
Limit for Limited 1	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension fraction to decimal: Include non-benchmark fractions to the thousandths place. (e.g., $\frac{7}{111} = 0.\overline{063}$ ) to conversions from decimals to fractions to the thousandths place. e.g., $0.\overline{123} = \frac{123}{999}$	Calculator Designation NO – a calculator will not be available for items

	Mathematics	8.NS.A.1.d
NS	Number Sense and Operations	
Α	Know that there are numbers that are not rational, and approximate them by rational numbers.	
1	Explore the real number system.	
d	Generate equivalent representations of rational numbers.	
	Expectation Unwrapped	DOK Ceiling
The stuc	ent will generate equivalent representations of rational numbers (fractions, decimals and percentages).	3 <u>Item Format</u> Selected Response Constructed Response Technology Enhanced
		Sample Stems
Include 1	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension ractions beyond the benchmark fractions.	Calculator Designation NO – a calculator will not be available for items

	Mathematics	8.NS.A.2
NS	Number Sense and Operations	
Α	Know that there are numbers that are not rational, and approximate them by rational numbers.	
2	Estimate the value and compare the size of irrational numbers and approximate their locations on a number lin	ie.
	Expectation Unwrapped	DOK Ceiling
The stud	ent will estimate the decimal representation of an irrational number (e.g. $\pi \sqrt{2}$ , $\sqrt{3}$ , etc.)	3
The stud		Item Format
The stud	ent will compare rational and irrational numbers (e.g., $\pi$ , $\sqrt{2}$ , $\sqrt{3}$ , <i>etc</i> . ) and approximate their locations on a	Selected Response
number	line.	Technology Enhanced
		Sample Stems
		<u>Sample Stems</u>
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
		NO – a calculator will not be
Limit est	imation of irrational numbers to less than the square root of one hundred.	available for items
Exclude	all tractions with a radical in the numerator or denominator.	
Exclude		

	Mathematics	8.EEI.A.1
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
1	Know and apply the properties of integer exponents to generate equivalent expressions.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will be able to simplify an expression that contains two or more terms with the same base being multiplied	3
by addin	g the integer exponents.	Item Format
,		Selected Response
The stud	ent will be able to simplify an expression that contains two or more terms with the same base being divided by	Constructed Response
subtracti	ng the integer exponents.	
The stud	ent will be able to simplify an expression that contains a power raised to another power by multiplying the	Sample Stems
integer e	xponents.	
The state		
multiplic	ative inverse.	
The stud	ent will be able to generate an equivalent expression containing a base raised to the power of zero by	
converti	ng to one.	
The stud	ent will know any base raised to a power of zero will simplify to be one.	
The stud	ent will know that the multiplication and division properties will only work when the base is the same.	
Only nur	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension neric bases (no variables)	<u>Calculator Designation</u>
Answers	should be in exponential form to truly assess if the student can apply the property.	may not be available for items
Include e	expressions with more than one operation.	

	Mathematics	8.EEI.A.2.a
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
2	Investigate concepts of square and cube roots.	
а	Solve equations of the form $x^2 = p$ and $x^3 = p$ , where p is a positive rational number.	
	Expectation Unwrapped	DOK Ceiling
<b>T</b> L		3
The stud	ent will use square root symbols to represent solutions to equations of the form $x^2 = p$ . $-16(x^2 - \frac{1}{16}\sqrt{16}, x - \frac{1}{4})$	Item Format
(e.g., x	$= 10, x = \pm \sqrt{10}, x = \pm \frac{1}{2}$	Selected Response
The stud	ent will use cube root symbols to represent solutions to equations of the form $x^3 = p$ .	Constructed Response
		Technology Enhanced
		Sample Stems
Limited t Limit the	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension op as positive rational number. square roots to less than or equal to six hundred twenty-five and cube roots to one thousand.	<u>Calculator Designation</u> NO – a calculator will not be available for items

	Mathematics	8.EEI.A.2.b
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
2	Investigate concepts of square and cube roots.	
b	Evaluate square roots of perfect squares less than or equal to 625 and cube roots of perfect cubes less than or	equal to 1000.
	Expectation Unwrapped	DOK Ceiling 3
The stud	ent will know square roots based on the perfect square.	Item Format
The stud	ent will know the cube root based on the perfect cube.	Selected Response Constructed Response
The stud	ents will know the square roots of perfect squares less than or equal to six hundred twenty-five.	
The stud	ents will know the cube roots of perfect cubes less than or equal to one thousand.	Sample Stems
Limit: sq than or e	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension uare roots of perfect squares less than or equal to six hundred twenty-five and cube roots of perfect cubes less equal to one thousand.	<u>Calculator Designation</u> NO – a calculator will not be available for items

	Mathematics	8.EEI.A.2.c
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
2	Investigate concepts of square and cube roots.	
С	Recognize that square roots of non-perfect squares are irrational.	
The stud	Expectation Unwrapped ent will know that square roots of non-perfect squares are irrational.	DOK Ceiling 3 Item Format
		Selected Response Constructed Response Technology Enhanced
		Sample Stems
Limit the	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension square roots of perfect squares less than or equal to six hundred twenty-five.	<u>Calculator Designation</u> NO – a calculator will not be available for items

	Mathematics	8.EEI.A.3
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
3	Express very large and very small quantities in scientific notation and approximate how many times larger one i	s than the other.
	Expectation Unwrapped	DOK Ceiling
		3
less than	ent will be able to express very large and very small quantities in scientific notation with the first factor written	Item Format
		Selected Response
Students	will know that a number multiplied by a base of ten raised to a positive exponent, the equivalent expression	Constructed Response
will resu	It in a larger number than the original factor.	Technology Enhanced
		Sample Stems
Students	will know that a number multiplied by a base of ten raised to a negative exponent will result in a smaller	
number	than the original factor.	
Students	will approximate how many times larger one expression (written in scientific notation) is than another	
expression	on (written in scientific notation).	
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
		<b>NO</b> – a calculator will not be
		available for items

	Mathematics	8.EEI.A.4.a
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
4	Use scientific notation to solve problems.	
а	Perform operations with numbers expressed in scientific notation, including problems where both decimal and	scientific notation are used.
	Expectation Unwrapped	DOK Ceiling
The stud (includin The stud	ent will be able to multiply two expressions written in scientific notation using integer exponent properties g where at least 1 expression is in scientific notation). ent will be able to divide two expressions written in scientific notation using integer exponent properties	Item Format Selected Response Constructed Response
(includin The stud	g where at least 1 expression is in scientific notation). ent will convert a number from standard notation into scientific notation to perform operations.	Sample Stems
The stud	ent will add or subtract two expressions written in scientific notation when the power of ten is the same.	
Answers Focus sh	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension should be written in scientific notation. ould be on multiplication and division and less on addition/subtraction.	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.EEI.A.4.b
EEI	Expressions, Equations and Inequalities	
Α	Work with radicals and integer exponents.	
4	Use scientific notation to solve problems.	
b	Use scientific notation and choose units of appropriate size for measurements of very large or very small quanti	ities.
	Expectation Unwrapped	DOK Ceiling
The stud	ent will use scientific notation to choose unit of appropriate size for measurement.	Item Format
Students	will be able to determine the most reasonable and appropriate unit of measure to use in a given situation.	Selected Response Constructed Response
Students	will use a calculator to input and interpret scientific notation.	lechnology Enhanced
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.EEI.B.5.a
EEI	Expressions, Equations and Inequalities	
В	Understand the connections between proportional relationships, lines and linear equations.	
5	Graph proportional relationships.	
а	Interpret the unit rate as the slope of the graph.	
	Expectation Unwrapped	DOK Ceiling 3
The stud	ent will interpret the unit rate (1, r) as the slope of the graph when given a proportional relationship.	Item Format
The stud	ent will be able to use the unit rate (1, r) to graph a proportional relationship that passes through the origin.	Selected Response Constructed Response
		Technology Enhanced
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Sample Stems
To assess ones.	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension s if students make the connection between slope and the unit rate, the scale on the x-axis needs to increase by	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.EEI.B.5.b
EEI	Expressions, Equations and Inequalities	
В	Understand the connections between proportional relationships, lines and linear equations.	
5	Graph proportional relationships.	
b	Compare two different proportional relationships.	
	Expectation Unwrapped	DOK Ceiling 3
The stud graphs a	ent will compare the slopes of two proportional relationships given multiple representations including tables, nd equations.	Item Format Selected Response Constructed Response Technology Enhanced
		Sample Stems
Values n	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension hay include integers and/or decimals and fractions that simplify to the hundredths place.	<u>Calculator Designation</u> YES – a calculator will be available for items
Values n	nay include integers and/or decimals and fractions that simplify to the hundredths place.	for items

	Mathematics	8.EEI.B.6.a	
EEI	Expressions, Equations and Inequalities		
В	Understand the connections between proportional relationships, lines and linear equations.		
6	Apply concepts of slope and y-intercept to graphs, equations and proportional relationships.		
а	Explain why the slope (m) is the same between any two distinct points on a non-vertical line in the Cartesian co	ordinate plane.	
	Expectation Unwrapped	DOK Ceiling	
The stue	ant will available why the clane (m) is the same between any two distinct points on a neg vertical line in the	3	
Cartesia	n coordinate plane.	Item Format	
		Selected Response	
		Constructed Response	
		Technology Enhanced	
		Sample Stems	
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation	
Values n	bay include integers and/or decimals and fractions that simplify to the hundredths place	YES – a calculator will be available	
values li	ay include integers and/or declinais and fractions that simplify to the hundredths plate.	IOI Items	

	Mathematics	8.EEI.B.6.b
EEI	Expressions, Equations and Inequalities	
В	Understand the connections between proportional relationships, lines and linear equations.	
6	Apply concepts of slope and y-intercept to graphs, equations and proportional relationships.	
b	Derive the equation y = mx for a line through the origin and the equation y = mx + b for a line intercepting the v	ertical axis at b.
	Expectation Unwrapped	DOK Ceiling
The stud	ent will write an equation in slope-intercept form when given a table of values.	ltem Format
The stud	ent will write an equation in slope-intercept form when given a linear graph.	Selected Response Constructed Response
The stud	ent will write an equation in slope-intercept form when given two-points on a line.	lechnology Enhanced
The stud	ent will write an equation in slope-intercept form when given a real-world linear situation.	Sample Stems
The stud	ent will write an equation in slope-intercept form when given the slope and the y-intercept of a line.	
The stud	ent will write an equation in slope-intercept form when given the slope and one-point on the line.	
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Values m	hay include integers and/or decimals and fractions that simplify to the hundredths place.	YES – a calculator will be available
When w	riting the equation from a graph, all coordinate pairs should be easily identifiable on intersecting grid lines.	for items

	Mathematics	8.EEI.C.7.a
EEI	Expressions, Equations and Inequalities	
С	Analyze and solve linear equations and inequalities and pairs of simultaneous linear equations.	
7	Solve linear equations and inequalities in one variable.	
а	Create and identify linear equations with one solution, infinitely many solutions or no solutions.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will give examples of linear equations with one solution, infinitely many solutions or no solutions.	3 Item Format
The stud	ent will identify linear equations with one solution, infinitely many solutions or no solutions.	Selected Response Constructed Response Technology Enhanced
		<u>Sample Stems</u>
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	<u>Calculator Designation</u> YES – a calculator will be available for items

	Mathematics	8.EEI.C.7.b
EEI	Expressions, Equations and Inequalities	
С	Analyze and solve linear equations and inequalities and pairs of simultaneous linear equations.	
7	Solve linear equations and inequalities in one variable.	
b	Solve linear equations and inequalities with rational number coefficients, including equations and inequalities w	hose solutions require expanding
	expressions using the distributive property and combining like terms.	
	Expectation Unwrapped	DOK Ceiling
The state		3
ne stud	and combining like terms	Item Format
property		Selected Response
The stud	ent will solve linear inequalities with rational number coefficients in one variable with or without the	Constructed Response
distribut	ve property and combining like terms.	Technology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Values m	ay include integers and/or decimals and fractions that simplify to the hundredths place.	YES – a calculator will be available
		for items

	Mathematics	8.EEI.C.8.a
EEI	Expressions, Equations and Inequalities	·
С	Analyze and solve linear equations and inequalities and pairs of simultaneous linear equations.	
8	Analyze and solve systems of linear equations.	
а	Graph systems of linear equations and recognize the intersection as the solution to the system.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will graph systems of linear equations.	3 Item Format
The stud	ent will recognize the intersection of two linear equations as the solution to a system.	Selected Response Constructed Response Technology Enhanced
		Sample Stems
The scale Limited t	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension e of the coordinate grid should allow for the y-intercept to be graphed on a scale value. to only two equations, both in slope-intercept form.	<u>Calculator Designation</u> NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.EEI.C.8.b
EEI	Expressions, Equations and Inequalities	
С	Analyze and solve linear equations and inequalities and pairs of simultaneous linear equations.	
8	Analyze and solve systems of linear equations.	
b	Explain why solution(s) to a system of two linear equations in two variables correspond to point(s) of intersection	on of the graphs.
	Expectation Unwrapped	DOK Ceiling
Tho stud	ant will avais why two lines that nover intersect will have no colution	3
The stud	ent win explain why two lines that never intersect win have no solution.	Item Format
The stud	ent will explain why two lines that intersect at all points will have infinitely many solutions.	Selected Response
		Technology Enhanced
The stud	ent will explain why two lines that intersect at one point will have one solution.	
When gi <sup>n</sup> able to e	ven a real-world context that can be modeled with a system of equations with one solution, the student will be xplain what the solution (x, y) values represent.	Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
		NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.EEI.C.8.c
EEI	Expressions, Equations and Inequalities	
С	Analyze and solve linear equations and inequalities and pairs of simultaneous linear equations.	
8	Analyze and solve systems of linear equations.	
С	Explain why systems of linear equations can have one solution, no solution or infinitely many solutions.	
	Expectation Unwrapped	DOK Ceiling 3
The stud solution.	ent will explain why two linear equations with the same slope and different y-intercepts would have no	Item Format Selected Response
The stud solutions	ent will explain why two linear equations with the same slope and y-intercept would have infinitely many 5.	Constructed Response Technology Enhanced
The stud	ent will explain why two linear equations with different slopes would have one solution.	Sample Stems
	State According on Content Limite /Doug device Classroom Work Should Include Sytemsion	Coloulator Designation
Students	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension may determine the number of solutions using a graph, analyzing for slopes/y-intercepts or solving the system.	<u>Calculator Designation</u> YES – a calculator will be available for items

	Mathematics	8.EEI.C.8.d
EEI	Expressions, Equations and Inequalities	
С	Analyze and solve linear equations and inequalities and pairs of simultaneous linear equations.	
8	Analyze and solve systems of linear equations.	
d	Solve systems of two linear equations.	
The stud	Expectation Unwrapped ent will solve systems of two linear equations in two variables algebraically.	DOK Ceiling 3 <u>Item Format</u> Selected Response Constructed Response Technology Enhanced <u>Sample Stems</u>
Students Both equ	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension may use substitution, elimination or inspection to solve systems. nations should be provided in the same form.	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.GM.A.1.a
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
1	Verify experimentally the congruence properties of rigid transformations.	
а	Verify that angle measure, betweenness, collinearity and distance are preserved under rigid transformations.	
	Expectation Unwrapped	DOK Ceiling
The stud translation	ent will verify that angle measures are preserved under rigid transformations of rotations, reflections, and ons.	Item Format Selected Response
The stud rigid trar	ent will verify that betweenness (the distance that point b is between point a and point c) is preserved under Isformations of rotations, reflections, and translations.	Constructed Response Technology Enhanced
The stud translatio	ent will verify that collinearity is preserved under rigid transformations of rotations, reflections, and ons.	Sample Stems
The stud	ent will verify that distance is preserved under rigid transformations of rotations, reflections, and translations.	
The stud reflection	ent will verify that any line (including parallel lines) transformed under a rigid transformation of rotation, n, or translation will still be a line.	
The stud congrue	ent will verify that after a rigid transformation of rotation, reflection, or translation, corresponding angles are nt.	
The stud segment	ent will verify that after a rigid transformation of rotation, reflection, or translation, corresponding line s are congruent.	
No more A sequer	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension than two rigid transformations performed at one time should be assessed. Ince of two transformations is limited to vertices of the original figure existing in the same quadrant including	Calculator Designation NEUTRAL – a calculator may or may not be available for items
the axes		

	Mathematics	8.GM.A.1.b
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
1	Verify experimentally the congruence properties of rigid transformations.	
b	Investigate if orientation is preserved under rigid transformations.	
	Expectation Unwrapped	DOK Ceiling
Invoction	to if orientation is preserved under rigid transformations	2
investiga	ate il orientation is preserved under rigid transformations.	Item Format
		Selected Response
		Constructed Response
		lechnology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.GM.A.2.a
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
2	Understand that two-dimensional figures are congruent if a series of rigid transformations can be performed to	o map the pre-image to the image.
а	Describe a possible sequence of rigid transformations between two congruent figures.	
	Expectation Unwrapped	DOK Ceiling
The stud reflection Given tw translatio	ent will understand that two-dimensional figures are congruent if a series of rigid transformations (rotations, ns, translations) can be performed to map the pre-image to the image. To congruent figures, the student will describe the sequence of rigid transformations (rotations, reflections, ons) that justifies the congruence between them.	3 Item Format Selected Response Constructed Response Technology Enhanced Sample Stems Calculator Designation
No more A sequer the axes. Limit rota	than two rigid transformations performed at one time should be assessed. The of two transformations is limited to vertices of the original figure existing in the same quadrant including The ations to 90°, 180°, 270°.	NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.GM.A.3
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry softwa	re.
3	Describe the effect of dilations, translations, rotations and reflections on two-dimensional figures using coor	dinates.
	Expectation Unwrapped	DOK Ceiling
The stud	ent will describe the effect of dilations on two-dimensional figures using coordinates	3
The stud	ent win desende the effect of diations of two dimensional figures doing coordinates.	Item Format
The stud	ent will describe the effect of rotations on two-dimensional figures using coordinates.	Selected Response
_		Technology Enhanced
The stud	ent will describe the effect of reflections on two-dimensional figures using coordinates.	
The stud	ent will describe the effect of translations on two-dimensional figures using coordinates.	Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Limit the	e center of rotation to a vertex of the figure or the origin.	YES – a calculator will be available
Limit rot	ations to 90°, 180°, 270°.	

	Mathematics	8.GM.A.4.a
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
4	Understand that two-dimensional figures are similar if a series of transformations (rotations, reflections, transl	ations and dilations) can be
	performed to map the pre-image to the image.	
а	Describe a possible sequence of transformations between two similar figures.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will understand that two-dimensional figures are similar if a series of rigid transformations (rotations,	ltone Formet
reflectio	ns, translations, and dilations) can be performed to map the pre-image to the image.	<u>Item Format</u>
		Constructed Response
Given tw translati	o similar figures, the student will describe the sequence of rigid transformations (rotations, reflections, ons, and dilations) that justifies the congruence between them.	Technology Enhanced
	State Accordment Content Limite/Boundaries Classroom Work Should Include Extension	Sample Stems
No more	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension than two transformations performed at one time should be assessed	<u>Calculator Designation</u> NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.GM.A.5.a
GM	Geometry and Measurement	·
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
5	Explore angle relationships and establish informal arguments.	
а	Derive the sum of the interior angles of a triangle.	
The stud	<b>Expectation Unwrapped</b> ent will establish informal arguments to derive the sum of the interior angles of a triangle.	DOK Ceiling 3 <u>Item Format</u> Selected Response Constructed Response
		Technology Enhanced
	State Accordment Content Limite/Boundaries Classroom Work Should Include Extension	Sample Stems
Students Values m Students angles)	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension are not required to give formal proofs at this point. hay include integers and/or decimals the tenths place. will not be required to identify angles by name at this level. (e.g., alternate interior angles, alternate exterior	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.GM.A.5.b
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
5	Explore angle relationships and establish informal arguments.	
b	Explore the relationship between the interior and exterior angles of a triangle.	
The stud	Expectation Unwrapped	DOK Ceiling 3
The stud triangle.	ent will establish informal arguments to explore the relationship between the interior and exterior angles of a	Item Format Selected Response Constructed Response Technology Enhanced
		Sample Stems
Students Values n Students angles)	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension are not required to give formal proofs at this point. hay include integers and/or decimals the tenths place. will not be required to identify angles by name at this level. (e.g., alternate interior angles, alternate exterior	<u>Calculator Designation</u> YES – a calculator will be available for items

	Mathematics	8.GM.A.5.c
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geo	ometry software.
5	Explore angle relationships and establish informal arguments.	
С	Construct and explore the angles created when parallel lines are cut by a transversal.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will construct narallel lines cut by a transversal	3
The stud		Item Format
The stud	ent will establish informal arguments to explore angles created when parallel lines are cut by	Selected Response
a transve	ersal.	Technology Enhanced
		Sample Stoms
		In the picture below, line m and line n are parallel. The
		measure of angle DCB is 48°. The measure of angle FAB is
		105°. What is the measure of angle CBA?
		C D m
		B
		F A E
Students	are not required to give formal proofs at this point.	<u>Calculator Designation</u> YES – a calculator will be available for items
Values n	hay include integers and/or decimals the tenths place.	
Students	will not be required to identify angles by name at this level. (e.g., alternate interior angles,	
alternate	e exterior angles)	

	Mathematics	8.GM.A.5.d
GM	Geometry and Measurement	
Α	Understand congruence and similarity using physical models, transparencies or geometry software.	
5	Explore angle relationships and establish informal arguments.	
d	Use the properties of similar figures to solve problems.	
The stud solve pro	Expectation Unwrapped ent will establish informal arguments to use properties (congruent corresponding angles) of similar figures to oblems.	DOK Ceiling 3 <u>Item Format</u> Selected Response Constructed Response Technology Enhanced <u>Sample Stems</u>
Students Values m Students angles)	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension are not required to give formal proofs at this point. hay include integers and/or decimals the tenths place will not be required to identify angles by name at this level. (e.g., alternate interior angles, alternate exterior	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.GM.B.6
GM	Geometry and Measurement	
В	Understand and apply the Pythagorean Theorem	
6	Use models to demonstrate a proof of the Pythagorean Theorem and its converse.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will use models to demonstrate a proof of the Pythagorean Theorem.	Jtom Format
The stud	ent will use models to demonstrate a proof of the converse of the Pythagorean Theorem.	Selected Response
Models	can include pictorial, graphic as well as equations.	Technology Enhanced
The stud	ent will use the Pythagorean Theorem to prove that three lengths can make a right triangle.	Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
values n	hay include integers and/or decimals.	for items

	Mathematics	8.GM.B.7	
GM	Geometry and Measurement		
В	Understand and apply the Pythagorean Theorem		
7	Use the Pythagorean Theorem to determine unknown side lengths in right triangles in problems in two- and thr	ee-dimensional contexts.	
	Expectation Unwrapped	DOK Ceiling	
The stud	ent will use the Pythagorean Theorem to determine unknown side lengths in right triangles in problems in two-	Itom Format	
dimensio	onal contexts.	Selected Response	
The stud	ent will use the Pythagorean Theorem to determine unknown side lengths in right triangles in problems in	Constructed Response	
three-di	nensional contexts.	Technology Enhanced	
		Sample Stems	
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension Calculator Designation		
Answers	could appear in non-simplified radical form.	YES – a calculator will be available	
		for items	

	Mathematics	8.GM.B.8
GM	Geometry and Measurement	
В	Understand and apply the Pythagorean Theorem	
8	Use the Pythagorean Theorem to find the distance between points in a Cartesian coordinate system.	
	Expectation Unwrapped	DOK Ceiling
The stud	lent will use the Pythagorean Theorem to find the distance between points in a Cartesian coordinate plane.	3
ine seue		Item Format
		Selected Response
		Technology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Values n	nay include integers and/or decimals.	YES – a calculator will be available
		for items

	Mathematics	8.GM.C.9.a
GM	Geometry and Measurement	·
С	Solve problems involving volume of cones, pyramids and spheres.	
9	Solve problems involving surface area and volume.	
а	Understand the concept of surface area and find surface area of pyramids.	
	Expectation Unwrapped	DOK Ceiling
The stud		3
The stud	ent will understand the concept of surface area of a pyramid.	Item Format
The stud	ent will find the surface area of a pyramid.	Selected Response
		Constructed Response
		rechnology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Pyramid	s will have a triangular or rectangular base.	YES – a calculator will be available
This may	r include a real-world context.	for items

	Mathematics	8.GM.C.9.b
GM	Geometry and Measurement	
С	Solve problems involving volume of cones, pyramids and spheres.	
9	Solve problems involving surface area and volume.	
b	Understand the concepts of volume and find the volume of pyramids, cones and spheres.	
	Expectation Unwrapped	DOK Ceiling
The stud	lent will understand the concept of volume of pyramids.	3
The stuc	lent will understand the concept of volume of cones.	Selected Response Constructed Response
The stud	lent will understand the concept of volume of spheres.	Technology Enhanced
The stud	lent will find the volume of pyramids.	Sample Stems
The stuc	lent will find the volume of cones.	
The stud	lent will find the volume of spheres.	
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Given m	easurements will be whole numbers.	<b>YES</b> – a calculator will be available
Will not	have composite figures.	for items
Answers		

	Mathematics	8.DSP.A.1
DSP	Data Analysis, Statistics and Probability	
Α	Investigate patterns of association in bivariate data.	
1	Construct and interpret scatter plots of bivariate measurement data to investigate patterns of association betw	een two quantities.
	Expectation Unwrapped	DOK Ceiling
The stud	ant will construct a coattor plot of hivariate measurement data	3
The stud	ent will construct a scatter plot of bivariate measurement data.	Item Format
The stud	ent will interpret a scatter plot of bivariate measurement data to identify clustering.	Selected Response
		Constructed Response Technology Enhanced
The stud	ent will interpret a scatter plot of bivariate measurement data to identify outliers.	
The stud	ent will interpret a scatter plot of bivariate measurement data to identify a positive or negative association.	Sample Stems
The stud	ent will interpret a scatter plot of bivariate measurement data to identify a linear or non-linear association.	
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Outliers	should be obscure enough to be identified through inspection.	NEUTRAL – a calculator may or
		may not be available for items

	Mathematics	8.DSP.A.2
DSP	Data Analysis, Statistics and Probability	
Α	Investigate patterns of association in bivariate data.	
2	Generate and use a trend line for bivariate data, and informally assess the fit of the line.	
	Expectation Unwrapped	DOK Ceiling 3
The stud	ent will understand that not all trend lines start at the origin.	Item Format
The stud	ent will know that not all trend lines pass through the data points.	Selected Response Constructed Response
The stud	ent will construct a line of best fit to model trends in a set of bivariate data.	Technology Enhanced
The stud	ent will use a straight line to model relationships between two quantitative variables for a scatter plot.	Sample Stems
The stud	ent will informally assess the fit of the line of best fit by evaluating the closeness of the data points to the line.	Calculator Designation
Students set. A line of least two	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension is should be able to explain that a line of best fit that is very close to the data points has a strong fit to the data best fit that is further from the data points has a weaker fit to the data set. On the graph the y-intercept and at o coordinate pairs must clearly fall on intersections of the coordinate grid lines.	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.DSP.A.3
DSP	Data Analysis, Statistics and Probability	
Α	Investigate patterns of association in bivariate data.	
3	Interpret the parameters of a linear model of bivariate measurement data to solve problems.	
	Expectation Unwrapped	DOK Ceiling
The stud	ent will use the equation for the line of best fit to solve problems in the context of a bivariate measurement	3
data set.		Item Format
The stud	ant will interpret the slape and wintercent in the line of best fit to calve problems in the context of a bivariate	Constructed Response
measure	ment data set.	Technology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Limit the	e coordinate grid to only the first quadrant.	<b>YES</b> – a calculator will be available
Values m	data set to ten values. Nav include integers and/or decimals and fractions that simplify to the hundredths place	for items
On the g	raph the y-intercept and at least two coordinate pairs must clearly fall on intersections of the coordinate grid	
lines.		

	Mathematics	8.DSP.A.4.a
DSP	Data Analysis, Statistics and Probability	
Α	Investigate patterns of association in bivariate data.	
4	Understand the patterns of association in bivariate categorical data displayed in a two-way table.	
а	Construct and interpret a two-way table summarizing data on two categorical variables collected from the same	e subjects.
	Expectation Unwrapped	DOK Ceiling 3
subjects.	ent will construct a two-way table summarizing data on two categorical variables collected from the same	Item Format Selected Response
The stud subjects.	ent will interpret a two-way table summarizing data on two categorical variables collected from the same	Technology Enhanced
		Sample Stems May want an example of a two-way table
Values m Column a	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension hay include integers and/or decimals and fractions that simplify to the hundredths place. and row totals should be shown on the tables.	<u>Calculator Designation</u> YES – a calculator will be available for items

	Mathematics	8.DSP.A.4.b
DSP	Data Analysis, Statistics and Probability	
Α	Investigate patterns of association in bivariate data.	
4	Understand the patterns of association in bivariate categorical data displayed in a two-way table.	
b	Use relative frequencies calculated for rows or columns to describe possible association between the two varial	bles.
Expectation Unwrapped		DOK Ceiling 3
The stud two varia	ent will use relative frequencies calculated for rows or columns to describe possible association between the ables.	Item Format Selected Response Constructed Response Technology Enhanced
		<u>Sample Stems</u>
Column	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension and row totals should be shown on the tables.	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.F.A.1.a
F	Functions	
Α	Define, evaluate and compare functions.	
1	Explore the concept of functions. (The use of function notation is not required.)	
а	Understand that a function assigns to each input exactly one output.	
	Expectation Unwrapped	DOK Ceiling 3
The stud	ent will understand that a function assigns every input (x-value) to exactly one output (y-value).	Item Format Selected Response Constructed Response Technology Enhanced
		Sample Stems
The use Values n Do not u	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension of function notation is not required. hay include integers and/or decimals and fractions that simplify to the hundredths place. se "domain" or "range" vocabulary.	Calculator Designation NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.F.A.1.b
F	Functions	·
Α	Define, evaluate and compare functions.	
1	Explore the concept of functions. (The use of function notation is not required.)	
b	Determine if a relation is a function.	
The stuc	Expectation Unwrapped	DOK Ceiling 3
diagram	, a set of ordered pairs, a table and/or a graph.	Item Format Selected Response Constructed Response Technology Enhanced
		Sample Stems
Multiple The use Values n	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension representations may include a mapping diagram, a set of ordered pairs, a table and/or a graph. of function notation is not required. nay include integers and/or decimals and fractions that simplify to the hundredths place.	<u>Calculator Designation</u> NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.F.A.1.c
F	Functions	
Α	Define, evaluate and compare functions.	
1	Explore the concept of functions. (The use of function notation is not required.)	
с	Graph a function.	
When gi	<b>Expectation Unwrapped</b> ven a set of input and output values, students will be able to graph a function on a coordinate grid.	DOK Ceiling 3 <u>Item Format</u> Selected Response
		Technology Enhanced
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Sample Stems
The use Values n	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension of function notation is not required. hay include integers and/or decimals and fractions that simplify to the hundredths place.	<u>Calculator Designation</u> NEUTRAL – a calculator may or may not be available for items

	Mathematics	8.F.A.2
F	Functions	-
Α	Define, evaluate and compare functions.	
2	Compare characteristics of two functions each represented in a different way.	
	Expectation Unwrapped	DOK Ceiling
The state		3
The stud	ent will compare the slope (rate of change) of two functions represented in a different way.	Item Format
The stud	ent will compare the y-intercept (initial value) of two functions represented in a different way.	Selected Response
		Constructed Response
		lechnology Enhanced
		Sample Stems
Values e	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
This com	marison will only address linear functions, 8 F A 3 will address non-linear vs. linear functions.	YES – a calculator will be available
		for items
Values n This com	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension hay include integers and/or decimals and fractions that simplify to the hundredths place. Inparison will only address linear functions. 8.F.A.3 will address non-linear vs. linear functions.	<u>Calculator Designation</u> YES – a calculator will be available for items

	Mathematics	8.F.A.3.a
F	Functions	·
Α	Define, evaluate and compare functions.	
3	Investigate the differences between linear and nonlinear functions.	
а	Interpret the equation y = mx + b as defining a linear function, whose parameters are the slope (m) and the y-in	tercept (b).
	Expectation Unwrapped	DOK Ceiling
The stud		3
The stud	ents will interpret the equation $y = mx + b$ as defining a linear function, whose graph is a straight line.	Item Format
The stud	ents will interpret that (m) represents the slope.	Selected Response
		Constructed Response
The stud	ents will interpret that (b) represents the y-intercept.	
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Values n	nay include integers and/or decimals and fractions that simplify to the hundredths place.	YES – a calculator will be available
		for items

	Mathematics	8.F.A.3.b
F	Functions	·
Α	Define, evaluate and compare functions.	
3	Investigate the differences between linear and nonlinear functions.	
b	Recognize that the graph of a linear function has a constant rate of change.	
	Expectation Unwrapped	DOK Ceiling 3
The stud	ent will recognize that the graph of a linear function has a constant rate of change.	Item Format Selected Response Constructed Response Technology Enhanced
		<u>Sample Stems</u>
This only intersect	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension addresses a graph of a linear function. Coordinate pairs must be clearly labeled with a point and fall on tions of the coordinate grid.	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.F.A.3.c
F	Functions	
Α	Define, evaluate and compare functions.	
3	Investigate the differences between linear and nonlinear functions.	
С	Give examples of nonlinear functions.	
The stud	<u>Expectation Unwrapped</u> dent will be able to give examples of a nonlinear function as a list of points, a table, a graph, an equation or a	DOK Ceiling 3
real world-context.		Item Format Selected Response Constructed Response Technology Enhanced
		Sample Stems
Respons	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension es should be limited to "nonlinear" without having to describe function.	<u>Calculator Designation</u> NEUTRAL – a calculator may or may not be available for items

Mathematics		8.F.B.4.a
F	Functions	
В	Use functions to model relationships between quantities.	
4	Use functions to model linear relationships between quantities.	
а	Explain the parameters of a linear function based on the context of a problem.	
	Expectation Unwrapped	DOK Ceiling
The stud given sit The stud situation	ent will explain that the slope is the constant rate of change and describe what this means in the context of a uation. ent will explain that the initial value is the y-intercept and describe what this means in the context of a given	3 Item Format Selected Response Constructed Response Technology Enhanced
		<u>Sample Stems</u>
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	<u>Calculator Designation</u> NEUTRAL – a calculator may or may not be available for items

Mathematics		8.F.B.4.b
F	Functions	·
В	Use functions to model relationships between quantities.	
4	Use functions to model linear relationships between quantities.	
b	Determine the parameters of a linear function.	
The stud tables, o	Expectation Unwrapped ent will determine the slope of a linear function given a description of the relationships or from two points, r graphs.	DOK Ceiling 3 <u>Item Format</u> Selected Response
The stud points, t	ent will determine the y-intercept of a linear function given a description of the relationships or from two ables, or graphs.	Constructed Response Technology Enhanced
		Sample Stems
Values n If the ite coordina	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension hay include integers and/or decimals and fractions that simplify to the hundredths place. m includes a graph, the coordinate pairs must be clearly labeled with a point and fall on intersections of the ite grid.	<u>Calculator Designation</u> YES – a calculator will be available for items

Mathematics		8.F.B.4.c
F	Functions	
В	Use functions to model relationships between quantities.	
4	Use functions to model linear relationships between quantities.	
с	Determine the x-intercept of a linear function.	
The stud The stud The stud ax+by=c	Expectation Unwrapped ent will identify an x-intercept from a graph and determine its meaning In the context of a given situation. ent will identify an x-intercept from a table and determine its meaning In the context of a given situation. ent will identify an x-intercept from an equation (e.g., in slope-intercept form y=mx+b or standard form and determine its meaning In the context of a given situation.	DOK Ceiling 3 <u>Item Format</u> Selected Response Constructed Response Technology Enhanced <u>Sample Stems</u>
Values m If the ite coordina	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension hay include integers and/or decimals and fractions that simplify to the hundredths place. m includes a graph, the coordinate pairs must be clearly labeled with a point and fall on intersections of the te grid lines.	Calculator Designation YES – a calculator will be available for items

	Mathematics	8.F.B.5
F	Functions	·
В	Use functions to model relationships between quantities.	
5	Describe the functional relationship between two quantities from a graph or a verbal description.	
	Expectation Unwrapped	DOK Ceiling
_		3
The student will describe the functional relationship between two quantities from a graph.		Item Format
The stud	ent will sketch a graph when given a description of the functional relationship.	Selected Response
		Constructed Response
		Technology Enhanced
		Sample Stems
	State Assessment Content Limits/Boundaries Classroom Work Should Include Extension	Calculator Designation
Descripti	ion of the functional relationship could include increasing/decreasing, linear/nonlinear. continuous/discrete.	<b>NEUTRAL</b> – a calculator may or
and/or c	onstant.	may not be available for items
Students	are not expected to calculate the average rate of change for a nonlinear or discontinuous function.	